Introduction to Adaptive Dynamics Theory

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Part C: Overview

What Are Function-Valued Traits?
Adaptive Dynamics of Function-Valued Traits
Example: Metabolic Investment Strategy
Example: Seasonal Flowering Schedule

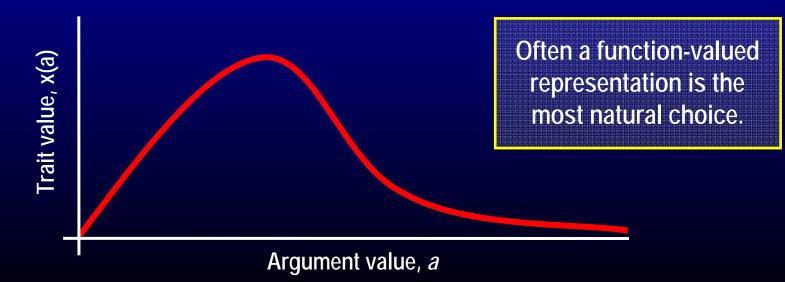


What Are Function-Valued Traits?

Function-Valued Traits

Adaptive traits in evolutionary ecology can be...

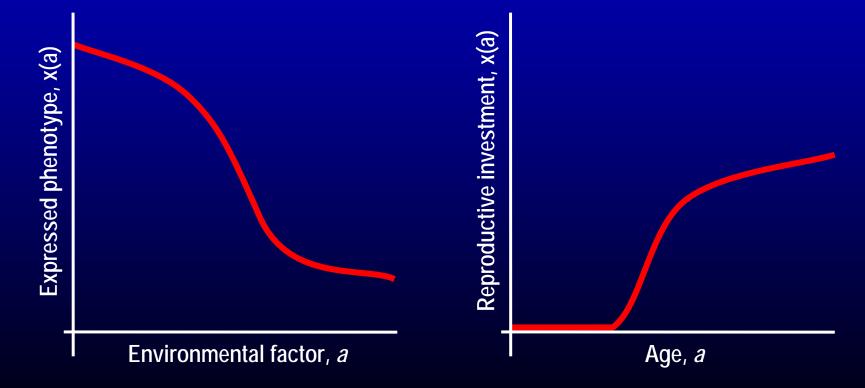
- Scalar xVectorial $(x_1, x_2, ..., x_n)$
- Function-valued x(a)



Examples of Function-Valued Traits 1 & 2

Reaction norms of phenotypic plasticity

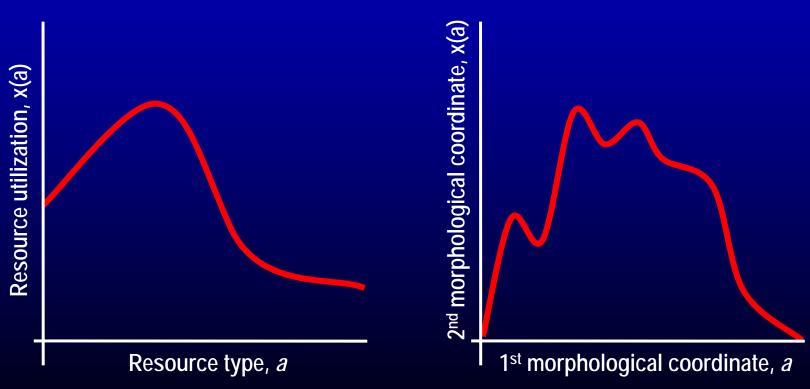
Demographic traits in structured populations



Examples of Function-Valued Traits 3 & 4

Resource utilization spectra

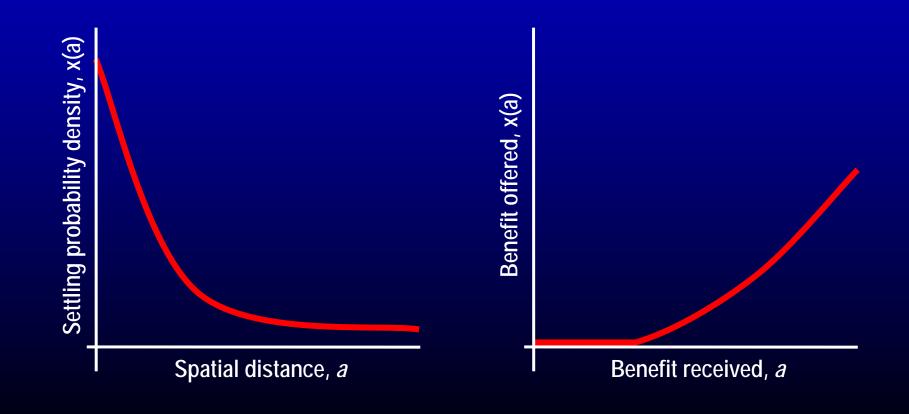
Morphological shapes



Examples of Function-Valued Traits 5 & 6

Dispersal kernels

Social interactions

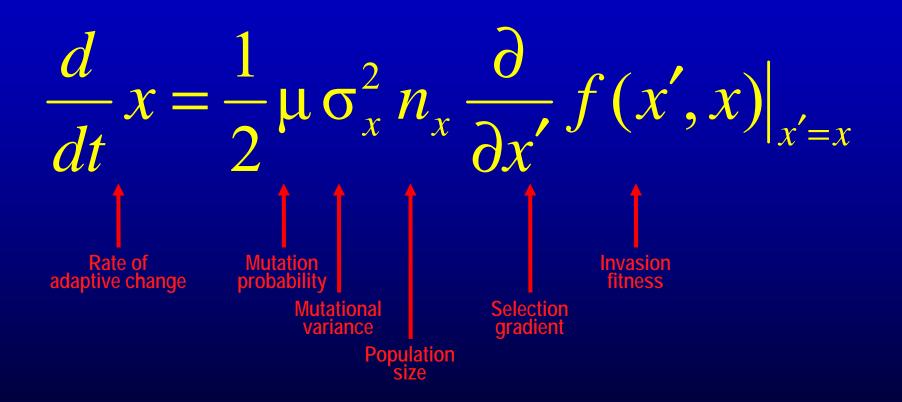




Adaptive Dynamics of FV Traits

Canonical Equation

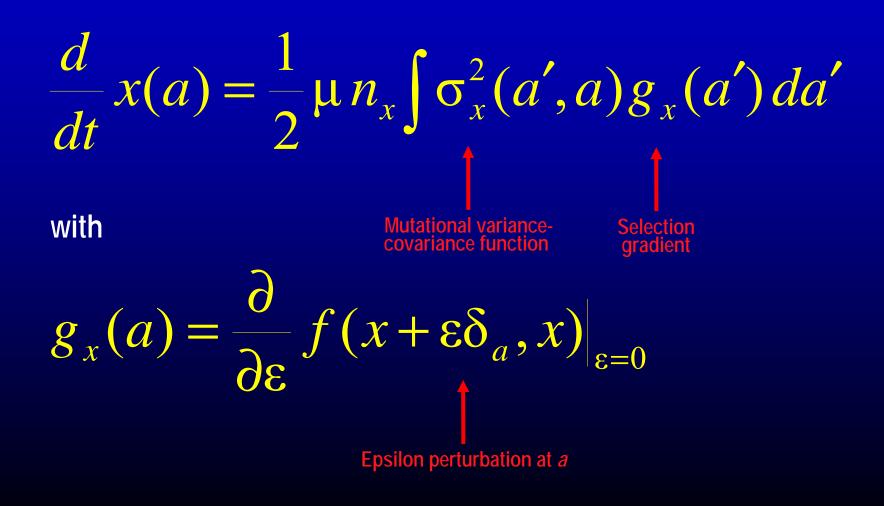
Dieckmann and Law (1996)



Dynamics amounts to hill-climbing on a variable adaptive landscape.

Dieckmann et al. (in press)

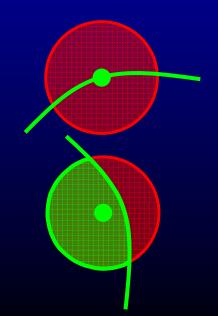
Canonical Equation for FV Traits



Adaptive Constraints on FV Traits

- Mutational variability may be unavailable, resulting in adaptive constraints.
- Two special cases are of particular interest. The mutation probability density $M_x(x)$ may be zero unless
 - F(x) = 0 (*equality* constraints):

• F(x') > 0 (*inequality* constraints):





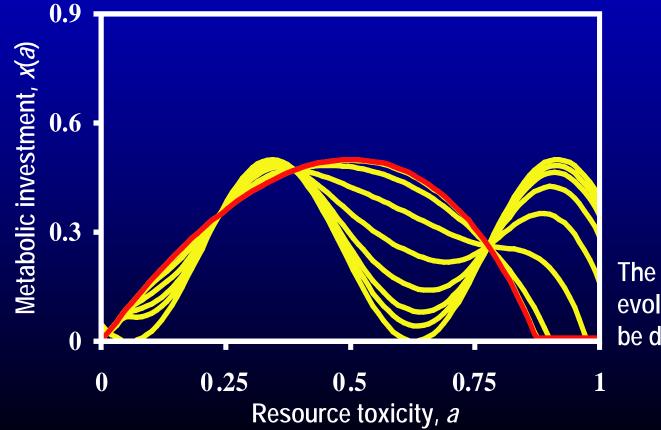
Evolution of a Metabolic Investment Strategy

First Example: Description

- We consider a consumer that harvests resources differing in toxicity *a*.
- The abundance of resources varies in proportion to, for instance, r(a)=4a(1-a).
- The consumer's metabolic efficiency increases with its investment x(a) according to e(a) = x(a)/[x(a)+a].
- Total gain is given by integrating r(a)e(a) over all a, and total costs are given by integrating cx(a) over all a.
- Net gain is obtained as total gain minus total costs.

First Example: Result

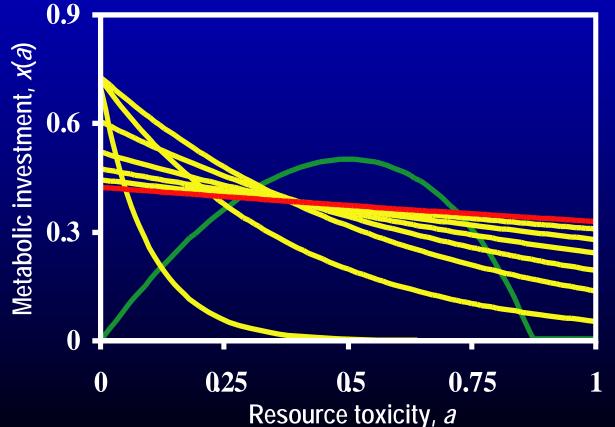
Transient dynamics and evolutionary attractor



The shape of the evolutionary attractor can be determined analytically.

The Dangers of Parametrization 1

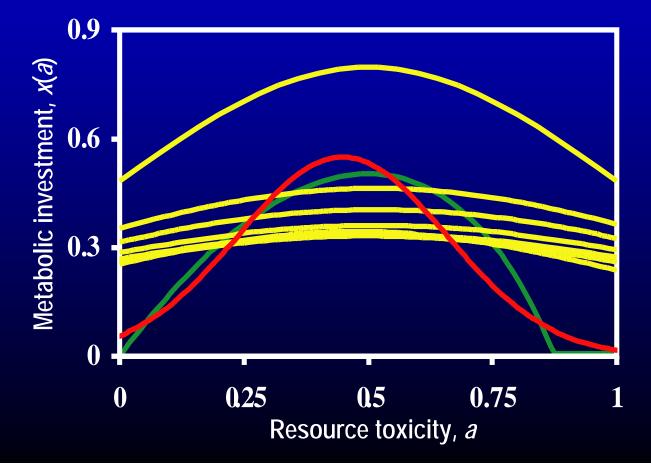
Exponential: Essentially irrelevant attractor



There is hardly any resemblance between the two evolutionary attractors.

The Dangers of Parametrization 2

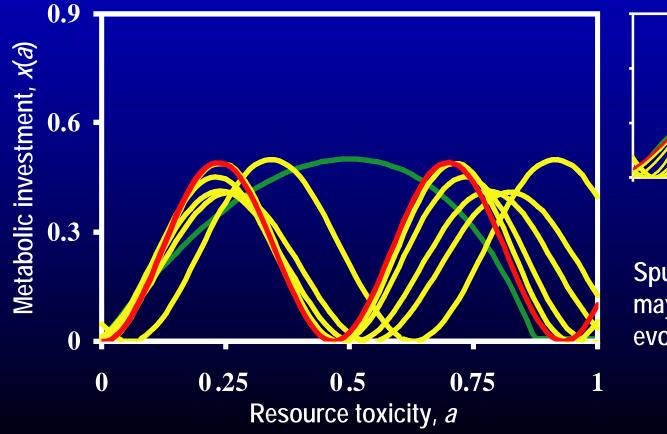
Normal: Qualitatively misleading attractor

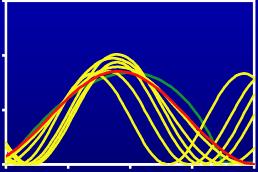


The asymmetry in the actual evolutionary outcome is missed.

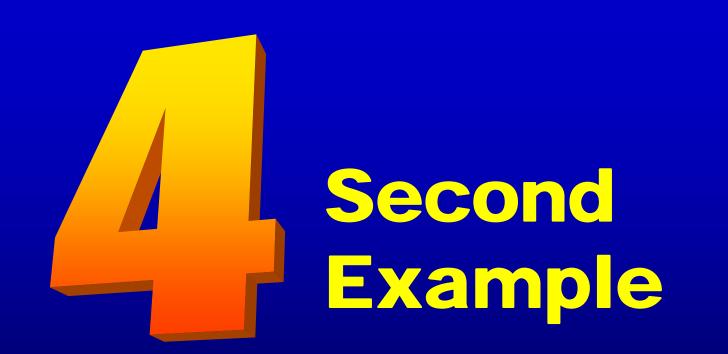
The Dangers of Parametrization 3

Sinusoidal: Spurious local evolutionary attractors





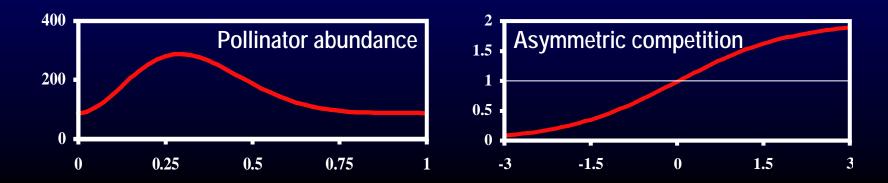
Spurious fitness valleys may stabilize spurious evolutionary attractors.



Evolution of a Seasonal Flowering Schedule

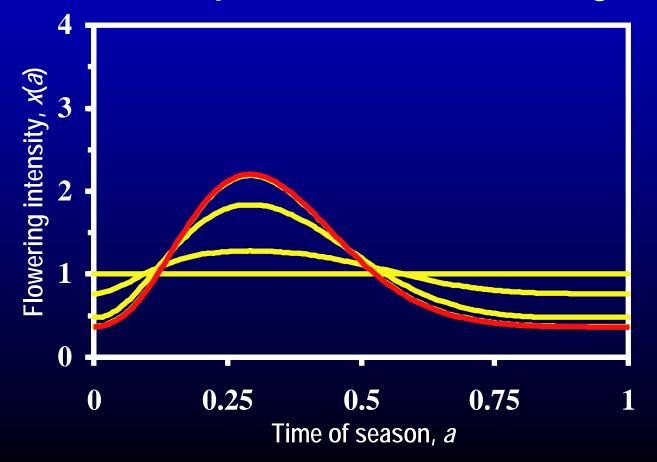
Second Example: Description

- We consider a plant that is exposed to a seasonally varying environment and at time *a* in the season exhibits a flowering intensity *x*(*a*).
- A certain total flowering intensity cannot be exceeded.
- The abundance of pollinators varies over the year, and plants compete asymmetrically for attracting these pollinators.



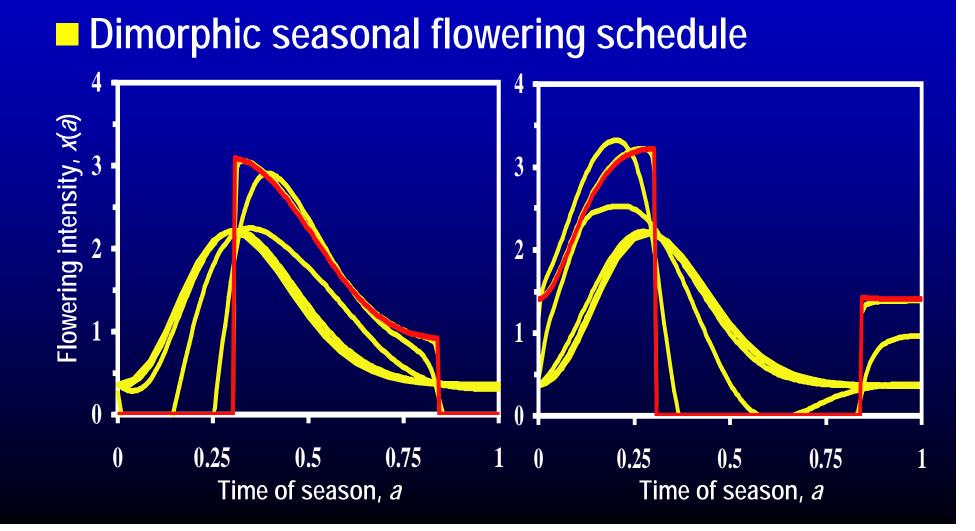
Second Example: Results

Monomorphic seasonal flowering schedule



Interestingly, this evolutionary attractor corresponds to a fitness minimum.

Evolutionary Branching of FV Traits



Function-Valued Traits: Summary

- Many phenotypes of interest in evolutionary ecology are best represented as function-valued traits.
- The long-term evolution of such traits can be studied using the canonical equation of adaptive dynamics theory.
- Frequency-dependent selection is readily encompassed.
- Equality and inequality constraints must receive particular attention.
- Evolutionary branching in function-valued traits opens up exciting opportunities for studying the interplay between individual-level plasticity and population-level diversity.